

# Fairness in Preference Queries: Social Choice Theories Meet Data Management

## Presenters:


























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\*NJIT, ^Ben Gurion University

Slides available at: <https://centers.njit.edu/bdal>

# Preference Queries

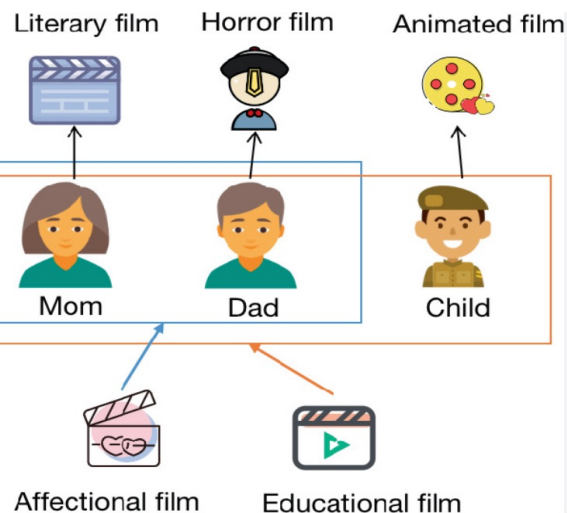
**Query: Which food is the most preferred choice?**

User	Preference								
Alex		>		>		>		>	
Bob		>		>		>		>	
Jill		>		>		>		>	
Jane		>		>		>		>	
Lia		>		>		>		>	

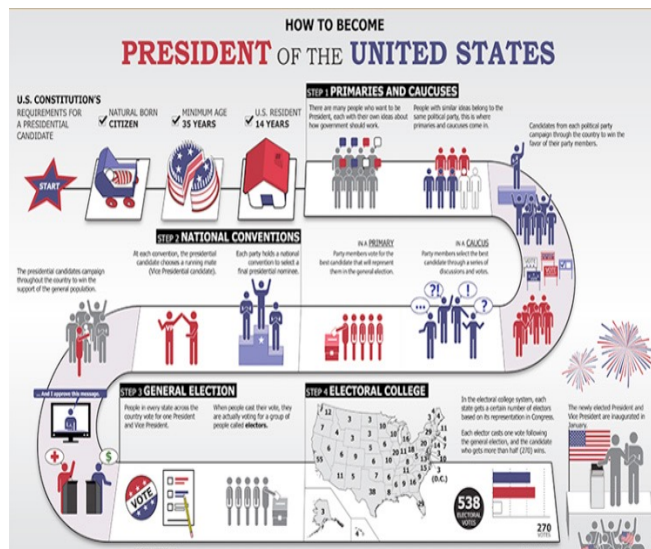
**Answer**



# Applications



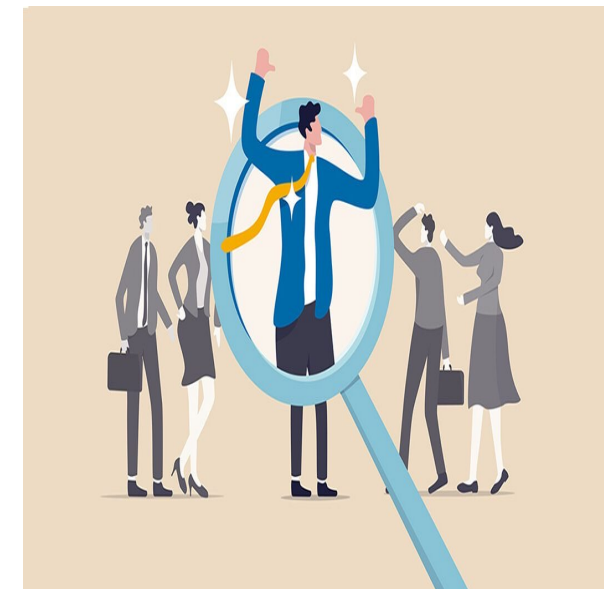
Group Recommendations



Electoral Systems



Hiring and recruitment



Admission

# Some More Applications



Sports competition  
Candidates  
shortlisting

Parliamentary elections  
Capacitated facility  
location

Company portfolio  
Movies selection  
Facility location



Application	Authors		
Querying	Lacroix and Lavency 1987; Kießling and Guntzer 1994; Köstler et al. 1995, Chomicki 2002; Kießling 2002; Kießling and Hafenrichter 2002; Kießling and Köstler 2002	Qualitative	the preferences between tuples in the answer to a query are specified directly, typically using binary preference relations
		Quantitative	preferences are specified indirectly using scoring functions that associate a numeric score with every tuple of the query answer.
Group Recommendation	Amer-yahia et. al., 2009; basu roy et. al. 2015, Yuan et. al. 2014,	Quantitative	Preferences are specified using scoring functions such as aggregated voting or least misery that associate a numeric score with every recommended item.

Notion of ranking is implicit!

# Overview



- Part I – Preference aggregation methods (30 minutes)
- Part II - Fairness in answering preference queries (30 minutes)
- Part III - Future research directions (20 minutes)

# Part I – Preference Aggregation Method (30 min)

## Plurality

(declare most loved one)

a

## Approval

(declare set of good ones)

[1,0,1]

## Ordinal

(order by preference)

a>b>c

## Cumulative

(distribute a token)

[0.5, 0.2, 0.3]

## Scoring

(score each option)

[3, 1, 5]



Voter	Ordinal Ballot
$V_1$	$b > a > c > d > e$
$V_2$	$e > a > b > d > c$
$V_3$	$d > a > b > c > e$
$V_4$	$c > b > d > e > a$
$V_5$	$c > b > e > a > d$

Given inputs (preference elicitation), an aggregation method (*voting rule*) outputs a single or multiple winner(s)

Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$
$v_2$	$e > a > b > d > c$
$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$

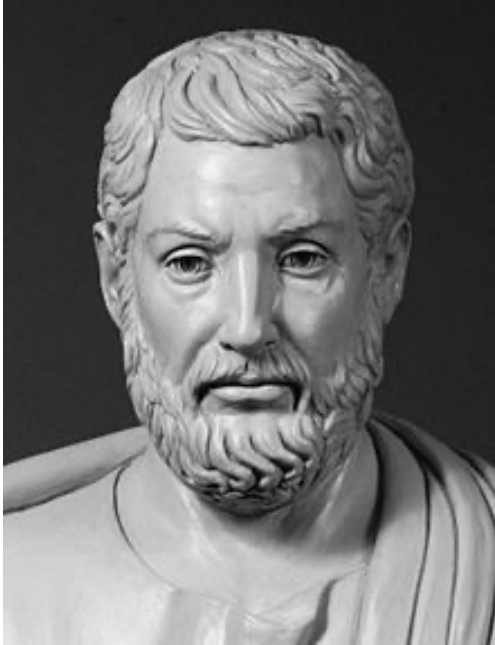
Any ideas?



Winners

Output

# Famous Aggregation Methods



Plurality / Sortition (~-500)



Llull (1299)



Condorcet (1785)



Borda (1770)



Dogdson (1876)



Shulze (1997)

Given an election, a voting rule outputs a single winner

Plurality: count 1<sup>st</sup> positions

Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$
$v_2$	$e > a > b > d > c$
$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$

$s(a) = 0$

$s(b) = 1$

$s(c) = 2$

$s(d) = 1$

$s(e) = 1$

1 0 0 0 0



Scoring vector

Given an election, a voting rule outputs a single winner

Plurality: count 1<sup>st</sup> positions

Borda: count (Borda) score

Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$
$v_2$	$e > a > b > d > c$
$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$

$s(a) = 10$

$s(b) = 14$

$s(c) = 11$

$s(d) = 8$

$s(e) = 7$

4 3 2 1 0

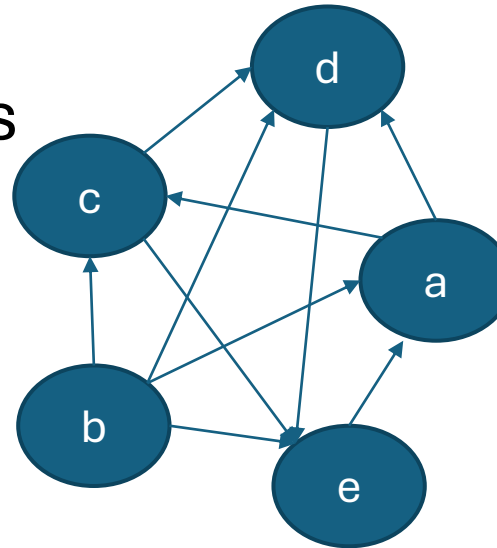
Scoring vector

Given an election, a voting rule outputs a single winner

Plurality: count 1<sup>st</sup> positions

Borda: count (Borda) score

Llull: count pairwise wins



Voter	Ordinal Ballot
v <sub>1</sub>	b > a > c > d > e
v <sub>2</sub>	e > a > b > d > c
v <sub>3</sub>	d > a > b > c > e
v <sub>4</sub>	c > b > d > e > a
v <sub>5</sub>	c > b > e > a > d

Given an election, a voting rule outputs a single winner

Plurality: count 1<sup>st</sup> positions

Borda: count (Borda) score

Llull: count pairwise wins

IRV: eliminate until majority



Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$
$v_2$	$e > a > b > d > c$
$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$



# How to make a choice on how to make a choice?

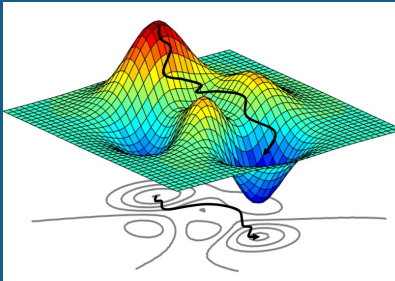
How to evaluate different voting rules?



# How to make a choice on how to make a choice?



## Optimization

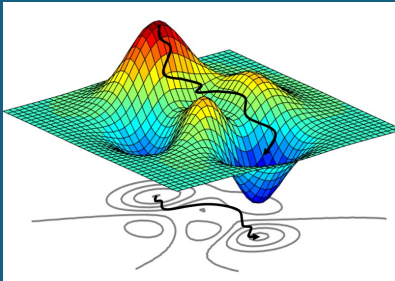


Defining  
optimization goals

# How to make a choice on how to make a choice?



## Optimization

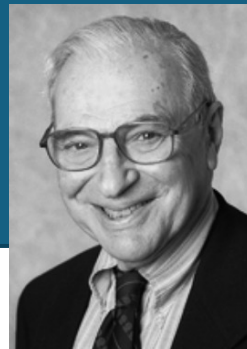


Defining  
optimization goals

## Axioms

Formulating good  
properties

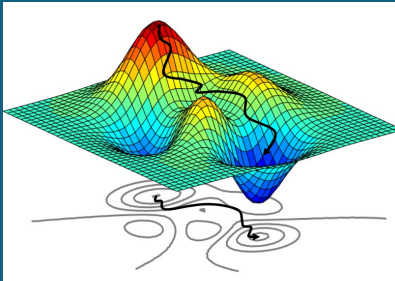
“My dream algorithm:  
proportional,  
discount monotone,  
etc...”



# How to make a choice on how to make a choice?



## Optimization

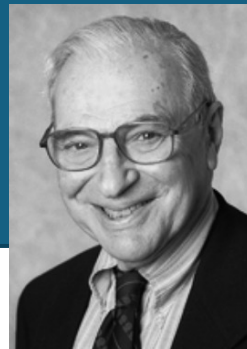


Defining  
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"My dream algorithm:  
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## Simulations & Experiments

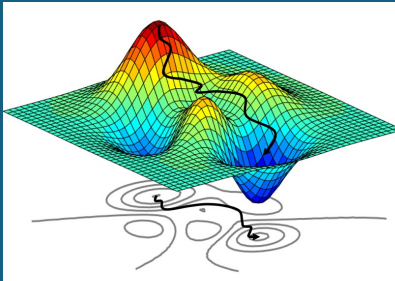
Does it  
look good?



# How to make a choice on how to make a choice?



## Optimization



Defining  
optimization goals

## Axioms

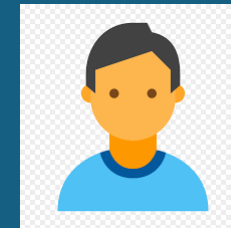
Formulating good  
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“My dream algorithm:  
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## Simulations & Experiments

Does it  
look good?

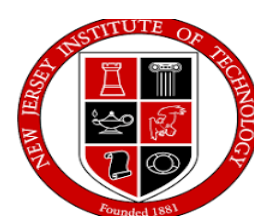


## Complexity and Xplainability



Ease of use..

# The Axiomatic Way



Let's formulate axioms expressing desirable (fairness) properties

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## Anonymity

voter names do not matter

Voter	Ordinal Ballot		Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$	↔	$v_1$	$e > a > b > d > c$
$v_2$	$e > a > b > d > c$		$v_2$	$b > a > c > d > e$
$v_3$	$d > a > b > c > e$		$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$		$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$		$v_5$	$c > b > e > a > d$

Let's formulate axioms expressing desirable (fairness) properties

## Neutrality

candidate names do not matter

Voter	Ordinal Ballot
$v_1$	$b > a > c > d > e$
$v_2$	$e > a > b > d > c$
$v_3$	$d > a > b > c > e$
$v_4$	$c > b > d > e > a$
$v_5$	$c > b > e > a > d$

Voter	Ordinal Ballot
$v_1$	$\mathbf{a} > \mathbf{b} > c > d > e$
$v_2$	$e > \mathbf{b} > \mathbf{a} > d > c$
$v_3$	$d > \mathbf{b} > \mathbf{a} > c > e$
$v_4$	$c > \mathbf{a} > d > e > \mathbf{b}$
$v_5$	$c > \mathbf{a} > e > \mathbf{b} > d$

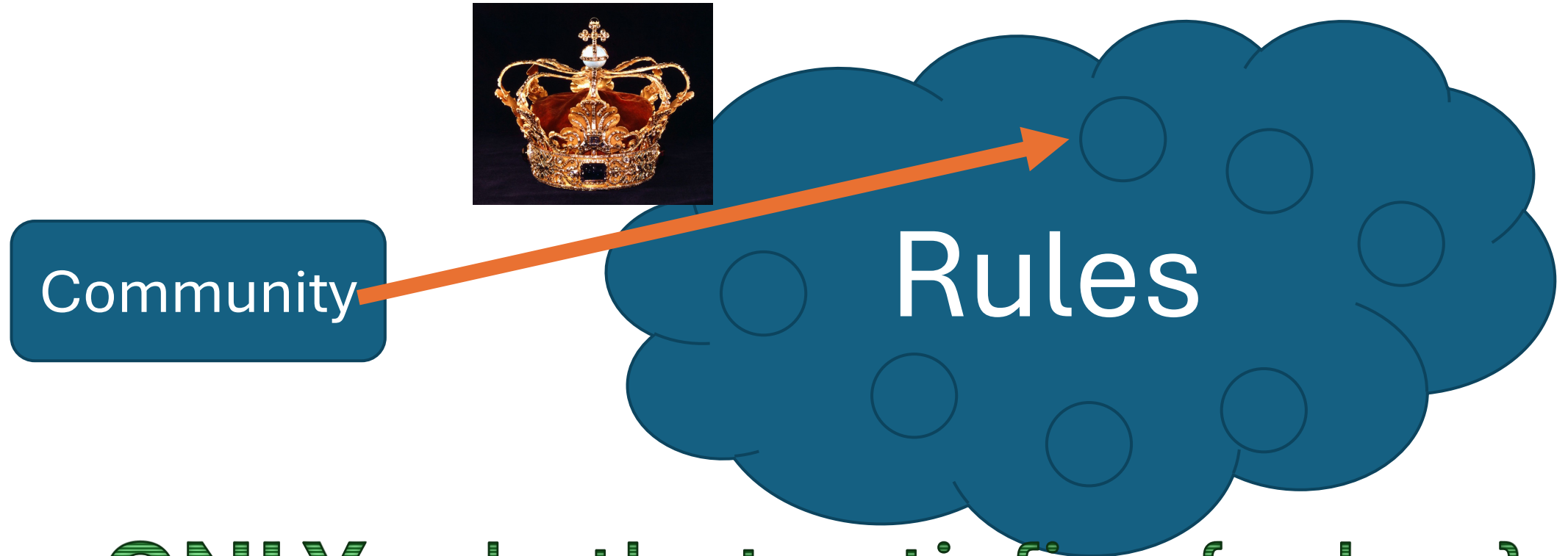
Let's formulate axioms expressing desirable (fairness) properties

**Positive Responsiveness (Monotonicity; campaigns don't hurt)**  
raised (tied) winner is winner

Voter	Ordinal ballots	Voter	Ordinal ballots
$v_1$	$a > b > c$	$v_1$	$b > a > c$
$v_2$	$a > b > c$	$v_2$	$b > a > c$
$v_3$	$b > a > c$	$v_3$	$b > a > c$
$v_4$	$b > a > c$	$v_4$	$b > a > c$

~~IRV~~





The **ONLY** rule that satisfies  $\{a, b, c\}$

## May's Theorem (1952):

A voting rule  $R$  for two alternatives satisfies:

anonymity, neutrality, and positive responsiveness

if and only if  $R$  is ???

simple majority

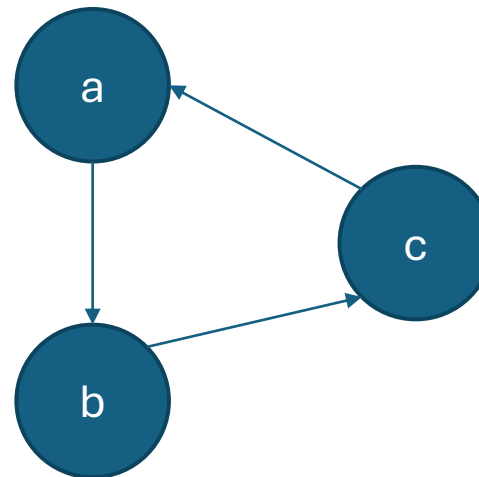
## Arrow's Impossibility Theorem (1951): No rule satisfies Pareto, IIA, and non-dictatorship

(Pareto – **a** dominates **b** if all voters prefer **a** to **b**; rule must select a non-dominated winner)

(IIA – if **a** wins over **b** when **c** is considered then **a** wins over **b** also when **c** is not considered)

(Non-dictatorship – not one voter dictates the output)

Voter	Ordinal ballots
$v_1$	$a > b > c$
$v_2$	$b > c > a$
$v_3$	$c > a > b$

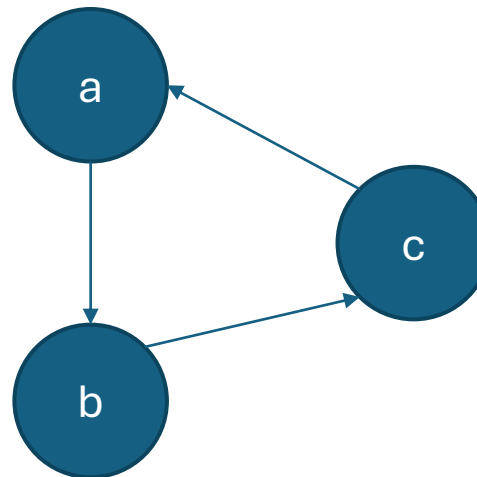


## GS Theorem (1973-5): No rule satisfies strategyproofness and non-dictatorship

(strategyproof – never beneficial to do strategic voting [i.e., to “lie”])

Voter	Ordinal ballots
$v_1$	$a > b > c$
$v_2$	$b > c > a$
$v_3$	$c > a > b$

Big Data Analytics Lab



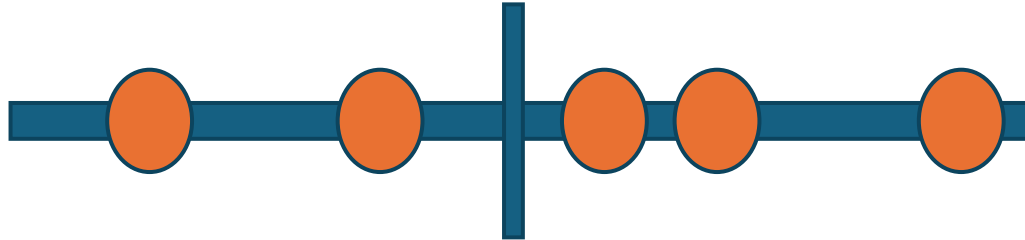
**Arrow's Theorem (1951):** No sane rule?

**GS Theorem (1973-5):** No strategyproof rule?

Not all is lost

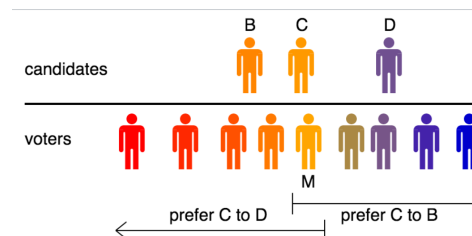
*Quantitative axioms!*  
*Randomization!*  
*Domain restrictions!*

**Black's Theorem (1948):** Median is strategyproof for singlepeaked domains

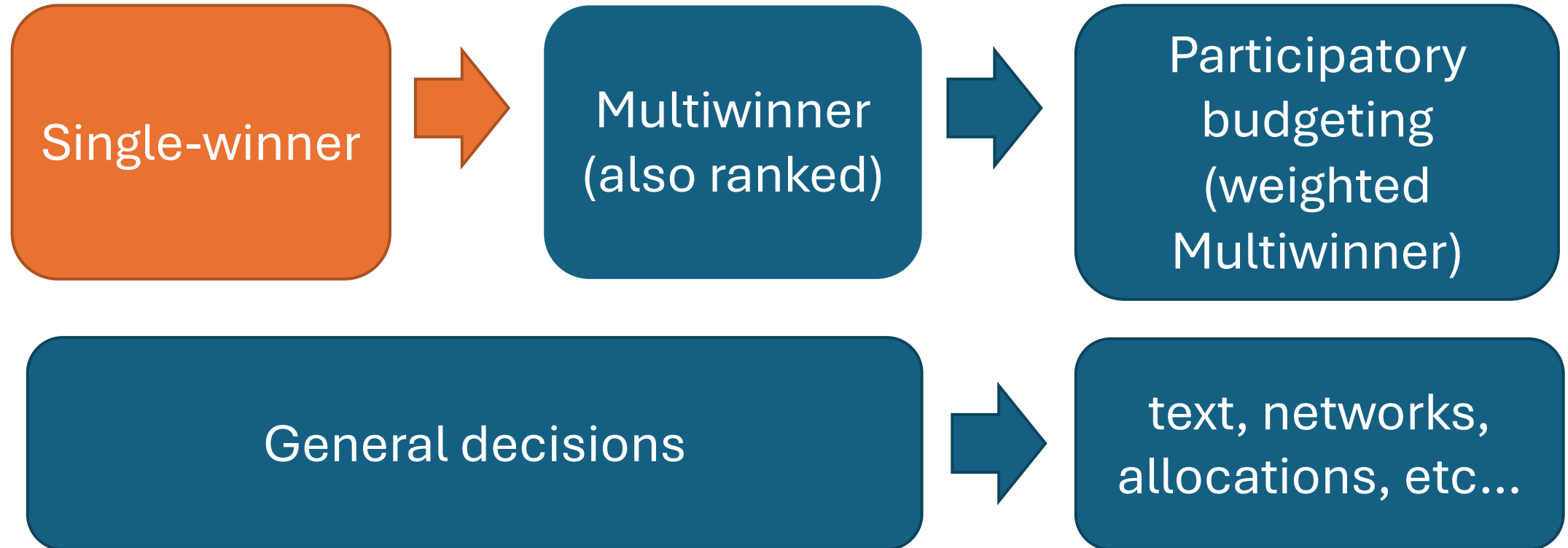


Center > Left > Right

~~Left > Right > Center~~



- Not just a single winner!



Topic	Paper	Essence
Proportional ranking	<a href="https://arxiv.org/pdf/1612.01434">https://arxiv.org/pdf/1612.01434</a>	Aggregate rankings to a single ranking while respecting minority opinion at all prefixes
Movie search via voting	<a href="https://arxiv.org/pdf/2202.03385">https://arxiv.org/pdf/2202.03385</a>	Using proportional multiwinner rules for group recommendation
Music recommendation by vote delegation	<a href="https://arxiv.org/pdf/1503.08604">https://arxiv.org/pdf/1503.08604</a>	Using dampened delegations for group recommendation
Clustering via social choice	<a href="https://arxiv.org/pdf/2310.18162">https://arxiv.org/pdf/2310.18162</a>	Being fair to the clusters by voting
Applicable fair division	Spliddit.org	Battle-tested fair division algorithms
Applicable sorition	Panelot.org	Battle-tested sortition app



# Summary:

## Single-Winner Voting Aggregation Methods

Aggregation method	Input format	Definition	Properties
Plurality	1-approval	Top-ranked candidate	Simple
Borda	ranking	Linear points	Average-best candidate
Approval	approval	Most approved	Avoids Arrow
IRV	Ranking (usually weak)	Eliminating and transferring until majority	Avoids certain strategic behaviors
Llull	ranking	Count pairwise wins	Picking Condorcet winner (candidate not losing in any pairwise contest)

# Summary:

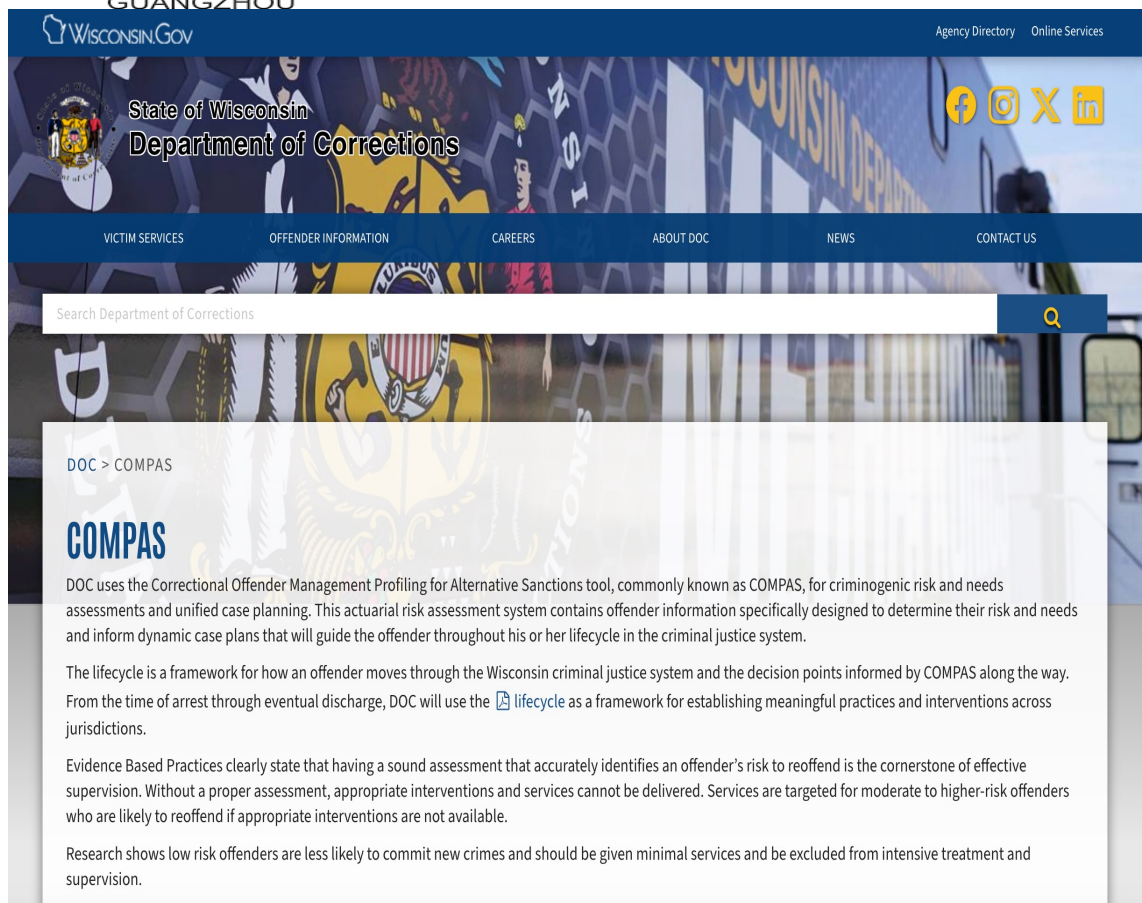
## Other Aggregation Methods



Aggregation method	Setting	Essence	Axiomatic properties	Computational properties
Kemeny	Social welfare function	Swap-closest ranking (centroid)		NP-hard (but efficient)
SNTV	Multiwinner	Top-ranked candidates	Not so great	P
k-Borda	Multiwinner	Average-ranked candidates	Picking candidates that are average-good	P
STV	Multiwinner	Eliminating and transferring until k seats	Picking a representative committee	P
Chamberlin-Courant	Multiwinner	Diverse committee	Most voters have at least one candidate they like	NP-hard (but theoretically-efficient)
Proportional approval voting (PAV)	Multiwinner	Representative minority-respecting committee	Picking a representative committee	NP-hard (but efficient)

# Part II – Existing Research on Fairness in Preference Queries (30 min)

**Algorithmic fairness** interprets fairness as lack of discrimination asking that an algorithm should not discriminate entities based on attributes that are not relevant to the task at hand. Such attributes are called **protected or sensitive**, and often include among others gender, religion, age, sexual orientation and race.



DOC > COMPAS

## COMPAS

DOC uses the Correctional Offender Management Profiling for Alternative Sanctions tool, commonly known as COMPAS, for criminogenic risk and needs assessments and unified case planning. This actuarial risk assessment system contains offender information specifically designed to determine their risk and needs and inform dynamic case plans that will guide the offender throughout his or her lifecycle in the criminal justice system.

The lifecycle is a framework for how an offender moves through the Wisconsin criminal justice system and the decision points informed by COMPAS along the way. From the time of arrest through eventual discharge, DOC will use the [lifecycle](#) as a framework for establishing meaningful practices and interventions across jurisdictions.

Evidence Based Practices clearly state that having a sound assessment that accurately identifies an offender's risk to reoffend is the cornerstone of effective supervision. Without a proper assessment, appropriate interventions and services cannot be delivered. Services are targeted for moderate to higher-risk offenders who are likely to reoffend if appropriate interventions are not available.

Research shows low risk offenders are less likely to commit new crimes and should be given minimal services and be excluded from intensive treatment and supervision.

## COMPAS Case Study: Investigating Algorithmic Fairness of Predictive Policing



Mallika Chawla · Follow

7 min read · Feb 23, 2022



44



The defendant, Eric Loomis, had been assessed by COMPAS (Correctional Offender Management Profiling for Alternative Sanctions) as a high risk individual and was consequently sentenced to eight years in prison — a ruling that he challenged as a violation of his due process rights.

Task	Work	What it does
Score based ranking	Measuring fairness in ranked outputs [Yang. et. al.]	proportional representation fairness within the NDCG framework, imposing proportionality constraint over every prefix of the ranking and accounting for position bias with a logarithmic discount.
Score based ranking	On obtaining stable rankings [Asudeh. et. al]	Proposes a framework that can be used to assess the stability of a provided ranking and to obtain a stable ranking within an “acceptable” range of weight values (called “the region of interest”)
Score based ranking	Designing Fair Ranking Schemes [Asudeh et. al.]	considers ranking functions that compute the score of each item as a weighted sum of (numeric) attribute values, and then sort items on their score. Each ranking function can be expressed as a point in a multidimensional space. For multiple fairness criteria, including proportionality, the work shows how to efficiently identify regions in this space that satisfy these criteria.
Range Queries	Fairness-Aware Range Queries for Selecting Unbiased Data [Shetiya et. al]	Query reformulation - finding the most similar fair range to a user-provided range query for the database to satisfy group fairness defined over a single binary protected attribute

Task	Work	What it does
Link analysis	Fairness-Aware PageRank [Tsioutsoulis et. al.]	Revisits Pagerank through the lens of fairness definition and study variants that are fair. The work defines the utility loss of a fair algorithm as the difference between its output and the output of the Pagerank algorithm, and it considers the problem of achieving fairness while minimizing utility loss.
Group recommendation	Fairness in Package-to-Group Recommendations [serbos et. al.]	Studies fairness aware package-to-group recommendations, that of fairness with the goal that every group member is satisfied by a sufficient number of items in the package.
Database repair	Interventional Fairness : Causal Database Repair for Algorithmic Fairness [Salimi et. al]	describes an approach to removing discrimination by repairing the training data in order to remove the effect of any discriminatory causal relationship between the protected attribute and classifier predictions, without assuming adherence to an underlying causal models.
Data structure design	FairHash: A Fair and Memory/Time-efficient Hashmap [Shahbazi et. al]	a data- dependant hashmap that guarantees uniform distribution at the group-level across hash buckets, and hence, satisfies the statistical parity notion of group fairness.



But THIS tutorial studies  
fairness considering Different and Multiple  
preferences with the goal of producing a  
single output ....

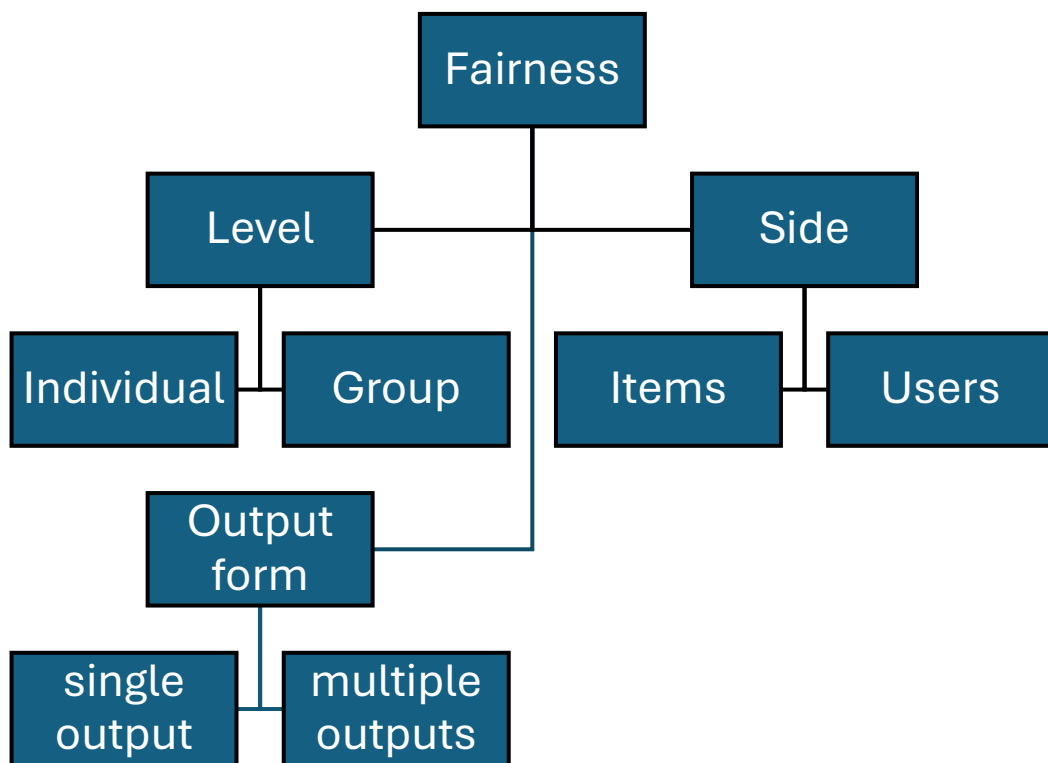


# Terminology



- Users(Voters) input preferences over items/candidates
- Input preferences are elicited differently
- Preference aggregation model takes inputs and generates output
  - Output is a
    - single item/candidate
    - a set of k items/candidates
    - a ranked order of items/candidates

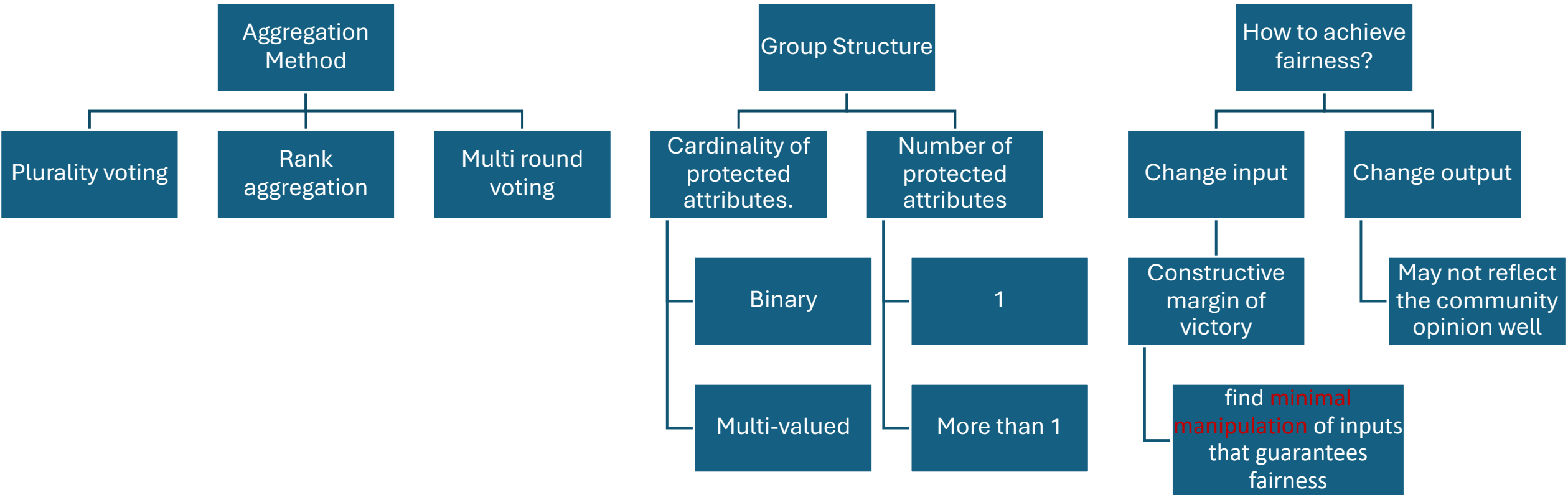
# A Possible Taxonomy of Fairness



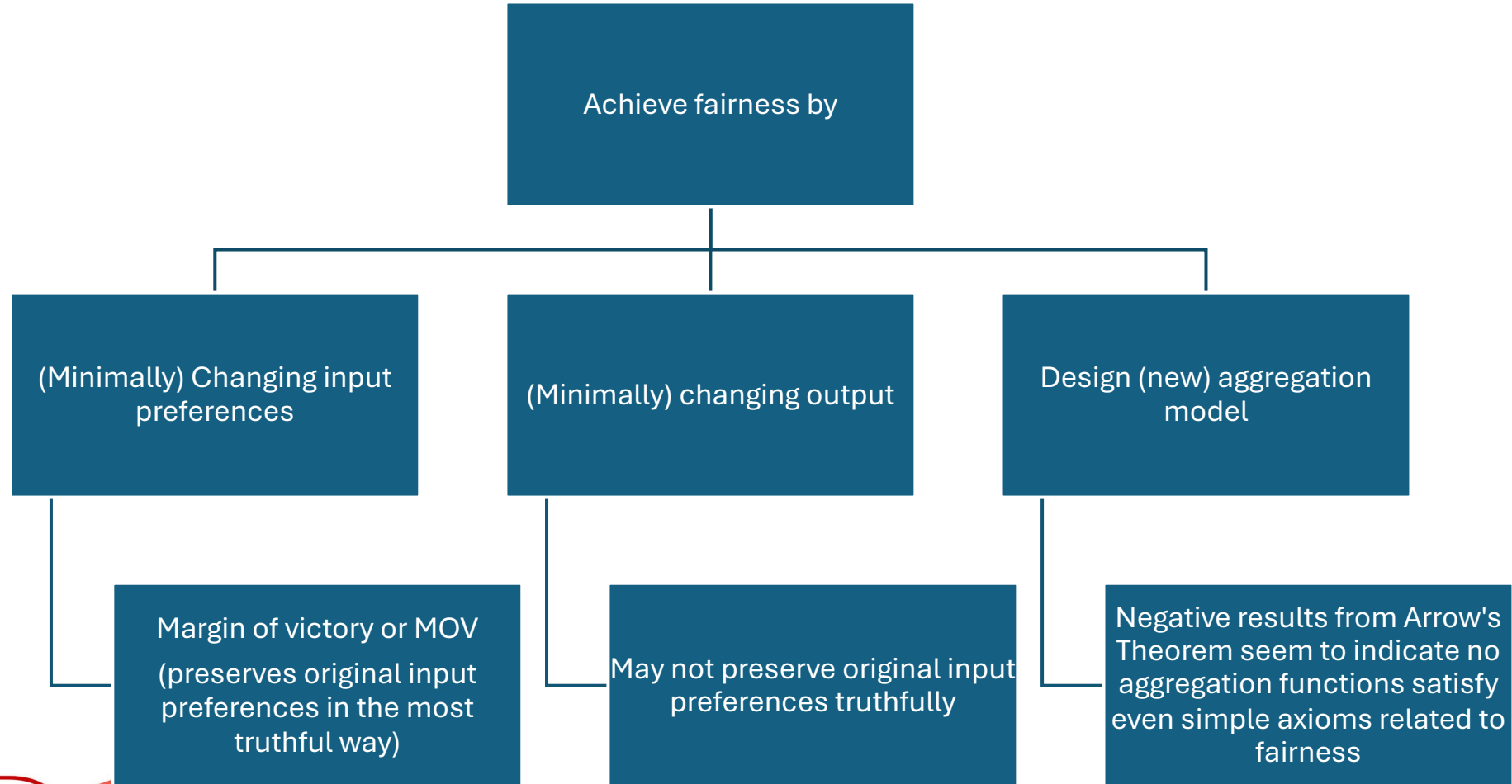
Type	Definition	
Level Based	Individual	Group
	Individuals with “similar” utility must have similar chance of getting favorable outcome	Members from different protected attribute groups must have equal chance of getting favorable outcome
Side Based	Items	User
	similar items receive similar favorable outcomes	Focuses on returning items to the users that express community interests and do not favor any specific user/ user group
Output forms	Single output	Multiple outputs
	One output (set/ordered) is produced to enable fairness	Multiple outputs are produced to achieve fairness

Fairness	Applicable to	Definition
Top-k Parity	Group Fairness	Proportionate representation of every protected attribute in top-k
p-fairness	Group Fairness	Proportionate representation of every protected attribute in <b>every prefix</b> of top-k
Probability-based fairness	Group fairness	defined by means of statistical significance tests that ask how likely it is that a given ranking was created by a fair process, such as by tossing a coin to decide whether to put a protected-group or a privileged-group item at position $i$
m-proportionality	Individual fairness	for what proportion of the users the output satisfies the following: there exists at least $m$ items in the output that each of those users like.
m-envyfreeness	Individual fairness	for what proportion of the users the output satisfies the following: for every such user, there exists at least $m$ items such that each item is in the top- $\delta\%$ of their preferences, for an input parameter $\delta$ .
Dissatisfaction fairness	Individual Fairness	Minimize maximum dissatisfaction across all the users in the community
Uniform selection probability	Individual Fairness	Items with similar "utility" have "equivalent" chance of exposure
N level pareto optimal	Individual Fairness	An output with $N$ items that are dominated by at most $N - 1$ other items. An item $j$ dominates another item $i$ if all users rank $j$ higher than $i$ .

# Computational Implications come from .....



# How to Achieve Fairness



# Rank Aggregation with Proportionate Fairness (SIGMOD 2022)

## **AUTHORS:**

Dong Wei, Md Mouinul Islam, Baruch Schieber, Senjuti Basu Roy

# Fair Rank Aggregation (NeurIPS 2022)

## **AUTHORS:**

D. Chakraborty, S. Das, A. Khan, A. Subramanian

# Rank aggregation of search engine outputs

- Dwork, Kumar, Naor, Sivakumar, “Rank aggregation methods for the web”, WWW, 2001.
  - Q: How can search-engine bias be overcome?
  - A: By combining results from multiple search engines

Search: Waterloo

## Google

1. Wikipedia: Battle of Waterloo
2. Wikipedia: Waterloo, ON
3. [www.city.waterloo.on.ca](http://www.city.waterloo.on.ca) (City of Waterloo website)
4. [www.uwaterloo.ca](http://www.uwaterloo.ca) (University of Waterloo)
5. [www.waterloorecords.com](http://www.waterloorecords.com)

## Yahoo!

1. [www.uwaterloo.ca](http://www.uwaterloo.ca)
2. Wikipedia: Battle of Waterloo
3. [www.city.waterloo.on.ca](http://www.city.waterloo.on.ca)
4. Wikipedia: Waterloo, ON
5. [www.waterloorecords.com](http://www.waterloorecords.com)

# Minimize the number of “disagreements”



## Aggregate ranking

1. [www.uwaterloo.ca](http://www.uwaterloo.ca) (4)
2. Wikipedia: Battle of Waterloo (1)
3. Wikipedia: Waterloo, ON (2)
4. [www.city.waterloo.on.ca](http://www.city.waterloo.on.ca) (3)

## Google

1. Wikipedia: Battle of Waterloo
2. Wikipedia: Waterloo, ON
3. [www.city.waterloo.on.ca](http://www.city.waterloo.on.ca)
4. [www.uwaterloo.ca](http://www.uwaterloo.ca)

## Yahoo!

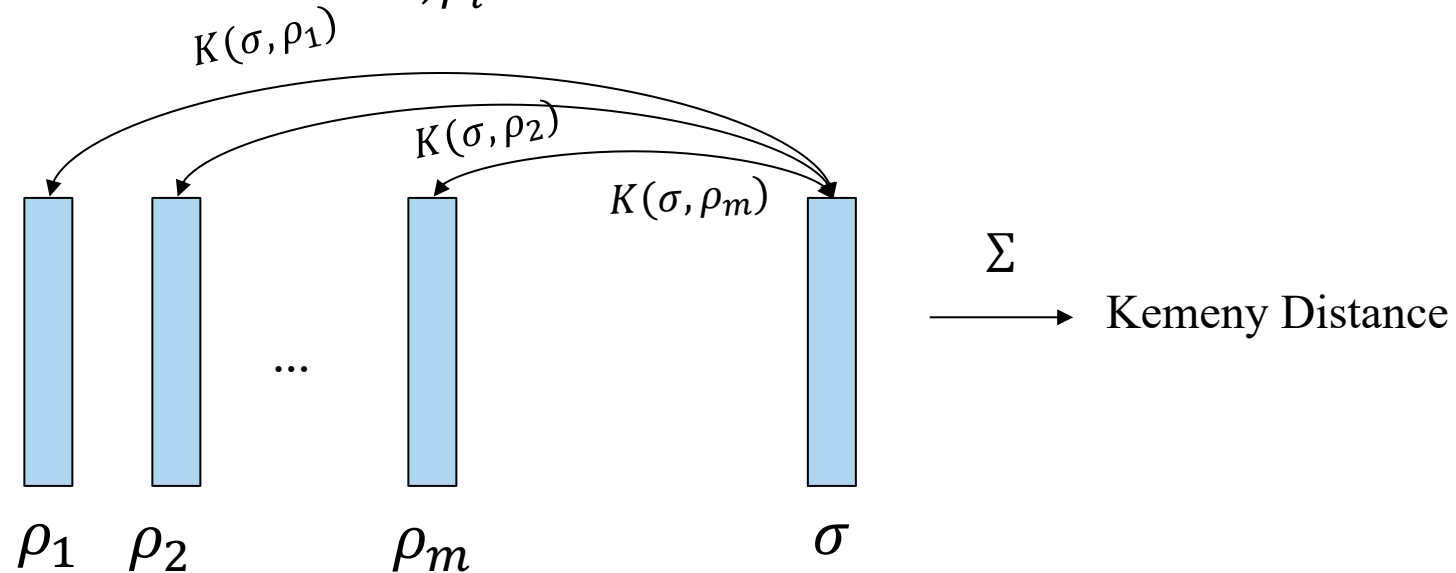
1. [www.uwaterloo.ca](http://www.uwaterloo.ca) (4)
2. Wikipedia: Battle of Waterloo (1)
3. [www.city.waterloo.on.ca](http://www.city.waterloo.on.ca) (3)
4. Wikipedia: Waterloo, ON (2)



**Kemeny Distance.** For rankings  $\rho_1, \rho_2, \dots, \rho_m$ , the Kemeny Distance of the ranking  $\sigma$  to these rankings is

$$\kappa(\sigma, \rho_1, \rho_2, \dots, \rho_m) = \sum_{i=1}^m K(\sigma, \rho_i)$$

$K(\sigma, \rho_i)$  = Kendall Tau distance between  $\sigma, \rho_i$



# Why Kemeny Distance



- Kemeny distance is a maximum likelihood estimator of the true preference order
- Simultaneously satisfies
  - Neutrality
    - $\kappa(\sigma_x, \rho_1, \rho_2, \dots, \rho_m) = \kappa(\rho_1, \rho_2, \dots, \rho_m, \sigma_x)$
  - Consistency
    - $\kappa(\sigma, \rho_1) + \kappa(\sigma, \rho_2) = \kappa(\sigma, (\rho_1, \rho_2))$
  - Condorcet winner property
    - If there is a candidate that wins majority of the preference, then that candidate wins
- Metric distance satisfies the triangle inequality
  - $K(\sigma, \eta) \leq K(\sigma, \eta') + K(\eta', \eta)$
- Has been studied extensively in rank aggregation literature [9,10]

[9] Dwork, Cynthia, et al. "Rank aggregation methods for the web." *Proceedings of the 10th international conference on World Wide Web*. 2001.

[10] Ailon, Nir, Moses Charikar, and Alantha Newman. "Aggregating inconsistent information: ranking and clustering." *Journal of the ACM (JACM)* 55.5 (2008): 1-27.

Rank	Protected Attribute
Amy	Female
Molly	Female
Abigail	Female
Kim	Male
Lee	Male
Park	Male
.	.
.	.

**Binary Protected Attribute : Gender**

Rank	Protected Attribute
Amy	Caucasian
Park	Asian
Molly	Caucasian
Kabir	Asian
Abigail	Native Hawaiian
Lee	Asian
.	.
.	.

**Multi-valued Protected Attribute : Race**

- $p$  = protected attribute value
- $f(p)$  = fraction of items with  $p$
- for every  $k \in [1..n]$ , the number of items with protected attribute value  $p$  is  $\lfloor f(p) \cdot k \rfloor$  or  $\lceil f(p) \cdot k \rceil$

F(female) = 50%

k	Min	Max
1	0	1
2	1	1
3	1	2

Aggregated Rank	Protected Attribute
Amy	Female
Park	Male
Molly	Female

K=1

Female = 1

K=2

Female = 1

K=3

Female = 2

P-fair Rank

## Applications

- Worker selection, Faculty hiring, School and college admission, medical residency

# p-fair Ranking

Proportionate representation in *every position*



50% male, 50% female

Rank	Protected Attribute	
Amy	Female	1 male, 1 female in top 2 position
Molly	Female	
Abigail	Female	
Kim	Male	2 male, 2 female in top 4 position
Lee	Male	
Park	Male	3 male, 3 female in top 6 position
.	.	
.	.	

Not p-fair

Rank	Protected Attribute	
Amy	Female	1 male, 1 female in top 2 positions
Park	Male	
Molly	Female	2 male, 2 female in top 4 positions
Kabir	Male	
Abigail	Female	3 male, 3 female in top 6 positions
Lee	Male	
.	.	
.	.	

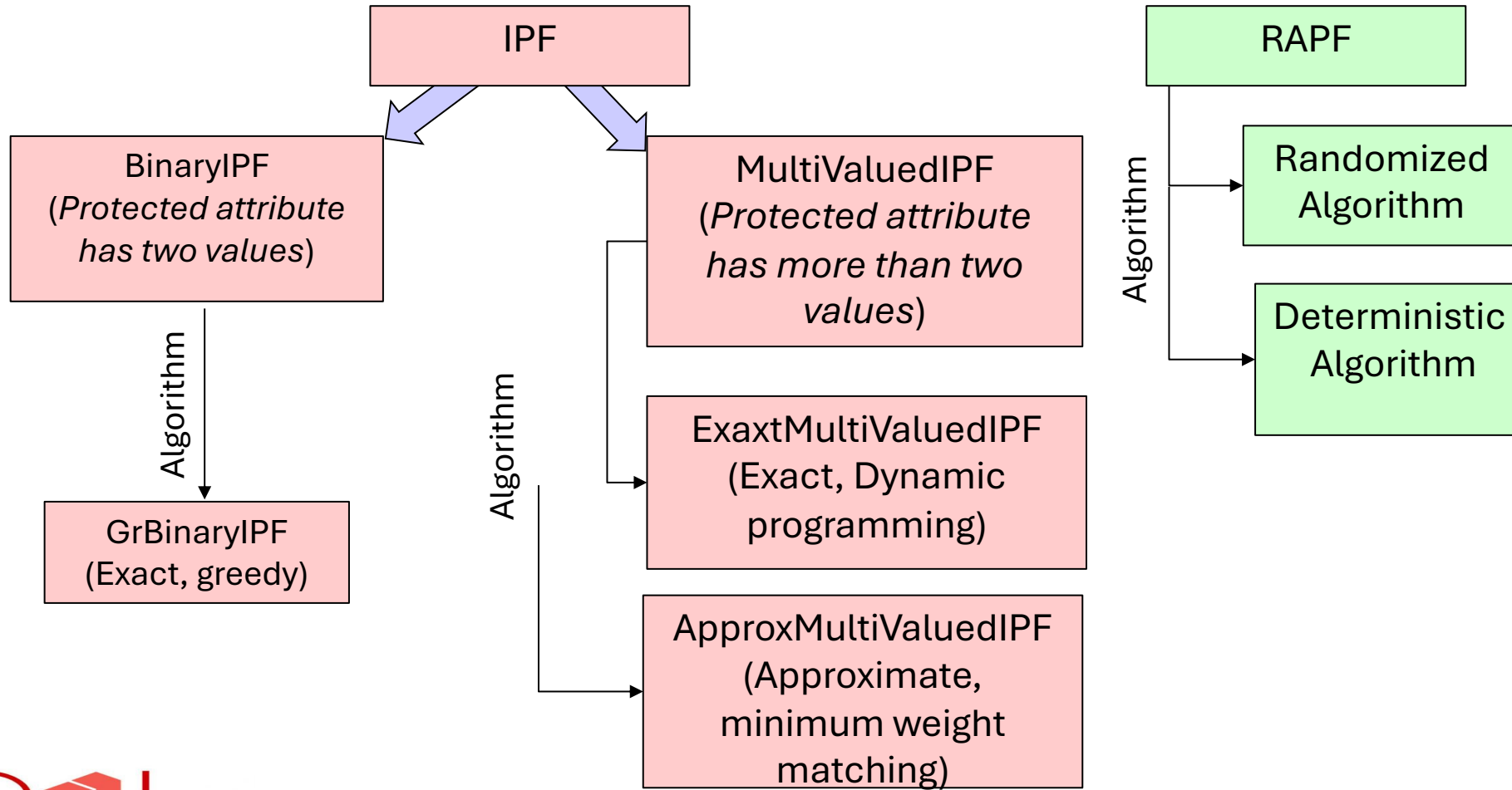
p-fair

# Problem Definitions



- **Individual p-fair rank** (or IPF). *Given a ranking  $\rho$  find a  $p$ -fair ranking that is closest to  $\rho$  in Kendall-Tau distance*
- **Rank aggregation under p-fairness** (or RAPF). *Given  $m$  rankings  $\rho_1, \rho_2, \dots, \rho_m$  find a  $p$ -fair ranking that minimizes the Kemeny distance to these  $m$  rankings*

# Studied Problems



Fairness in a single rank		Fairness in Rank Aggregation	
DetConstSort [3]	IPF	FairILP[4]	RAPF
Does not produce a p-fair ranking (only satisfies the lower bound of p-fairness)	Satisfies p-fairness.	Does not ensure p-fairness (Only satisfy pairwise statistical parity constraint)	Satisfy p-fairness.
Does not produce the closest ranking that satisfies the p-fairness lower bound	GrBinaryIPF, ExactMultiValuedIPF produces closest p-fair ranking.	Produces closest ranking that satisfy pairwise statistical parity constraint.	Does not produce the closest ranking that satisfies p-fairness.
Does not provide theoretical guarantees	<b>Exact solutions</b> GrBinaryIPF, ExactMultiValuedIPF  <b>2-approximation factor</b> ApproxMultiValuedIPF	Exact algorithm	<b>2-approximation factor</b> RAPF(binary) <b>3-approximation factor</b> RandAlgRAPF+ ExactMultiValuedIPF <b>4-approximation factor</b> RandAlgRAPF+ ApproxMultiValuedIPF
Computationally scalable.	Computationally scalable.	Computationally not scalable.	Computationally scalable.



# Satisfying Complex Top- $k$ Fairness Constraints by Preference Substitutions (VLDB 2023)

## AUTHORS:

Md Mouinul Islam, Dong Wei, Baruch Schieber, and Senjuti Basu Roy

# Top-k Selection via Plurality Voting



***Voters and candidates.  $m$  users (voters) provide top-1 preference over  $n$  candidates***

***Find  $k$  candidates with the  $k$  highest numbers of votes***

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12	Count
C1	1	1	0	1	0	0	1	0	0	0	0	0	4
C2	0	0	1	0	1	0	0	0	1	0	0	0	3
C3	0	0	0	0	0	1	0	0	0	0	0	1	2
C4	0	0	0	0	0	0	0	0	0	1	1	0	2
C5	0	0	0	0	0	0	0	1	0	0	0	0	1
C6	0	0	0	0	0	0	0	0	0	0	0	0	0

**If  $k=4$ , C1, C2, C3, C4 are the winners.**

**Query:** Find top-k (4) individuals with 2 males and 2 females (constraint on Gender) and 2 seniors and 2 juniors (constraint on Seniority Level) and 2 married, 1 single, and 1 divorced (constraint on Marital status)

**Query comes with one or more fairness constraints defined over one or more protected attributes**

Attribute	Value	Constraint
Gender <b>Binary attribute</b>	Male (M)	2
	Female (F)	2
Seniority Level <b>Binary attribute</b>	Senior (Sr)	2
	Junior (Jr)	2
Marital Status <b>Multivalued Attribute</b>	Married (ma)	2
	Single (si)	1
	Divorced (di)	1

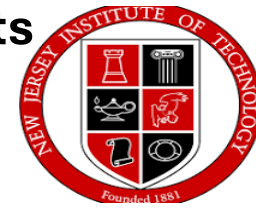
Candidate	Value
C1	M, Sr, si
C2	M, Jr, si
C3	M, Jr, ma
C4	F, Jr, si
C5	F, Jr, ma
C6	F, Sr, di

**The current top-4 candidates {C1, C2, C3, C4} DO NOT satisfy the query!!!**

# Preference (Ballot) Substitution to Satisfy Query Constraints

*Single Ballot substitution. Remove one vote from candidate*

*$i$  and assign it to candidate  $j$ ;*



- Perform 3 single ballot substitutions

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12	Count
C1 (M,Sr,si)	1	1	0	1	0	0	1	0	0	0	0	0	4
C2 (M,Jr,si)	0	0	1	0	1	0	0	0	1	0	0	0	3
C3 (M,Jr,ma)	0	0	0	0	0	1	0	0	0	0	0	1	2
C4 (F,Jr,si)	0	0	0	0	0	0	0	0	0	1	1	0	2
C5 (F,Jr,ma)	0	0	0	0	0	0	0	1	0	0	0	0	1
C6 (F,Sr,di)	0	0	0	0	0	0	0	0	0	0	0	0	0

—by removing 2 votes from C2 and 1 vote from C4

—assigning 2 votes to candidate C6 and 1 vote to C5.

- The resulting top-4 candidates (C1,C3,C5,C6) with votes (4, 2, 2, 2) satisfy fairness constraints.

**Single Ballot substitution.** Remove one vote from candidate

$i$  and assign it to candidate  $j$ ;

- Perform 3 single ballot substitutions

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12	Count
C1 (M,Sr,si)	1	1	0	1	0	0	1	0	0	0	0	0	4
C2 (M,Jr,si)	0	0	1	0	1	0	0	0	1	0	0	0	3
C3 (M,Jr,ma)	0	0	0	0	0	1	0	0	0	0	0	1	2
C4 (F,Jr,si)	0	0	0	0	0	0	0	0	0	1	1	0	2
C5 (F,Jr,ma)	0	0	0	0	0	0	0	1	0	0	0	0	1
C6 (F,Sr,di)	0	0	0	0	0	0	0	0	0	0	0	0	0

–by removing 2 votes from C2 and 1 vote from C4

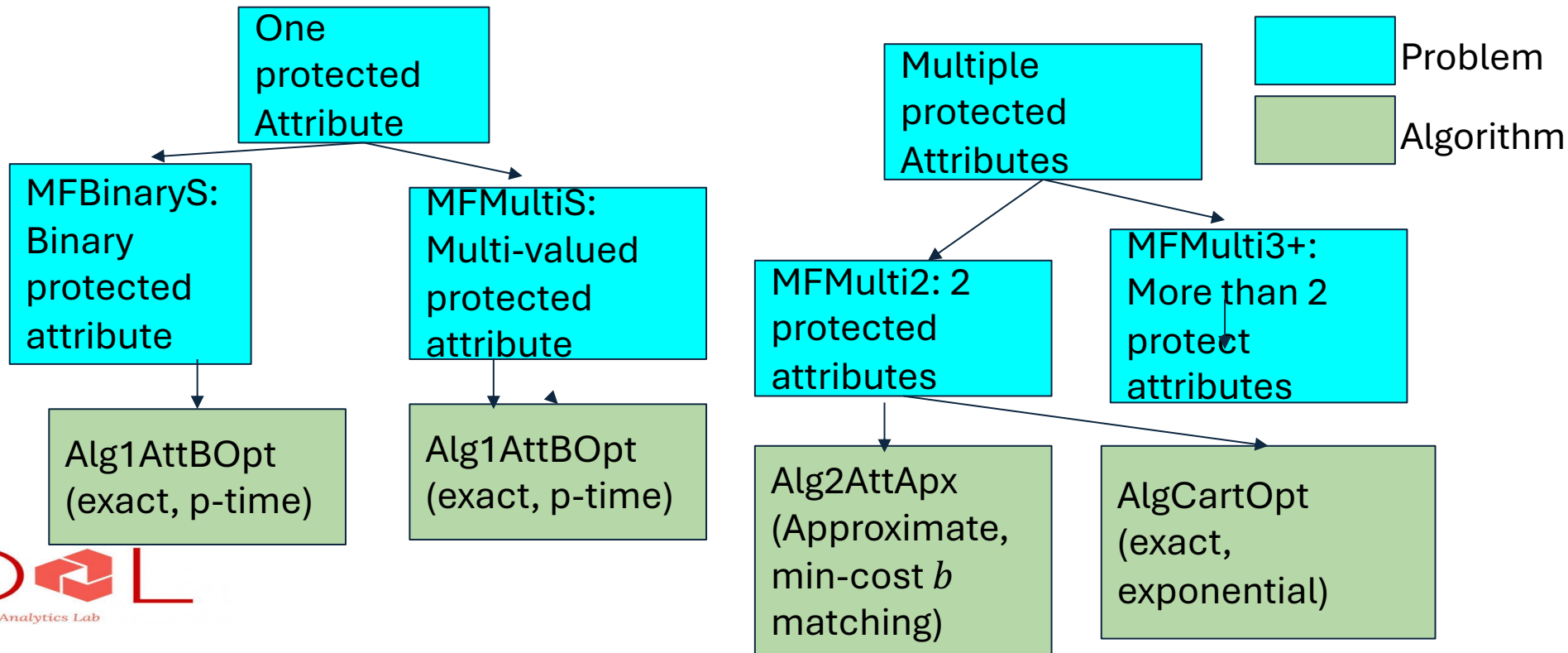
–assigning 2 votes to candidate C6 and 1 vote to C5.

- The resulting top-4 candidates (C1,C3,C5,C6) with votes (4, 2, 2, 2) satisfy fairness constraints.

# Problem definition

**Single ballot substitution.** Given two candidates  $i$  and  $j$ , a single ballot substitution is defined as removing one vote from candidate  $i$  and assigning it to candidate  $j$

**Margin.** Margin is the minimum number of single ballot substitutions needed to guarantee that the top- $k$  results satisfy the fairness constraints.



Subgroup fairness [3,4]		Margin finding problem [5,6,7]	
Existing solutions	Our Solution	Existing solutions	Our Solution
Studied primarily in the context of classification models to ensure that a classifier is fair not only on each individual group but also it stays fair when more structured subgroups are defined over the protected attributes.	Fairness constraints are imposed over multiple protected attributes and could be imposed over subgroups with the goal of returning top-k results that satisfy constraints.	Margin of victory is studied in electoral voting systems to understand robustness of an underlying voting mechanism, specifically for the Single Transferable Vote (STV).	Margin finding problem is studied in the context of plurality voting to satisfy complex fairness constraints.
Audit a fixed classifier to see if it satisfies subgroup fairness (i.e., the false positive rates are equivalent across all subgroups) is deemed to be computationally hard [4]	Margin finding problem for 2 attributes is NP-hard. Deciding the feasibility of a fair outcome for 3 or more attributes is NP-Complete.	Orlin and Bartholdi proved margin finding is NP-hard even for a single candidate selection for STV [5]	P-time solution for single protected attribute, NP-hard for multiple protected attribute
Heuristic solutions	Exact or approximate solutions	Fairness constraints are not considered	Fairness constraints are imposed

[3] Subgroup fairness. Michael Kearns, Seth Neel, Aaron Roth, and Zhiwei Steven Wu. 2019. An Empirical Study of Rich Subgroup Fairness for Machine Learning. In Proceedings of the Conference on Fairness, Accountability, and Transparency. ACM. <https://doi.org/10.1145/3287560.3287592>

[4] Michael J. Kearns, Seth Neel, Aaron Roth, and Zhiwei Steven Wu. Preventing fairness gerrymandering: Auditing and learning for subgroup fairness. In Jennifer G. Dy and Andreas Krause, editors, Proceedings of the 35th International Conference on Machine Learning, ICML 2018, Stockholm, Sweden, July 10-15, 2018, volume 80 of JMLR Workshop and Conference Proceedings, pages 2569–2577. JMLR.org, 2018. URL <http://proceedings.mlr.press/v80/kearns18a.html>

[5] John J Bartholdi and James B Orlin. 1991. Single transferable vote resists strategic voting. Social Choice and Welfare 8, 4 (1991), 341–354

[6] Michelle Blom, Peter J Stuckey, and Vanessa J Teague. 2017. Towards computing victory margins in STV elections. arXiv preprint arXiv:1703.03511 (2017)

[7] David Cary. 2011. Estimating the Margin of Victory for Instant-Runoff Voting. In 2011 Electronic Voting Technology Workshop/Workshop on Trustworthy Elections (EVT/WOTE 11).

# Promoting Fairness and Priority in k-Winners Selection Using IRV (KDD 2024)

## **AUTHORS:**

Md Mouinul Islam, Soroush Vahidi, Baruch Schieber, and Senjuti Basu Roy



## • Instant Run-off Voting (IRV):

- Tally the **first choice votes**
- The candidate that has the lowest number of first choice votes is **eliminated**. Ties are broken arbitrarily
- All the ranked orders that include the eliminated candidate are updated, and the candidates following this eliminated candidate are **advanced one place up**

					1	2	3	4	5	6	7	8	9	10
							Sara	Sara	Sara	Sara	Sara	Sara	Sara	Sara

- Faculty hiring committee ranking

1	2	3	4	5	6	7	8	9	10
Zoey	Laura	Zoey	Zoey	Mira	Sara	Gina	Sara	Kim	Laura
Mira	Gina	Molly	Molly	Molly	Gina	Sara	Gina	Gina	Kim
Laura	Molly	Kim	Sara	Sara	Kim	Kim	Kim	Sara	Gina
Gina	Kim	Gina	Gina	Kim	Zoey	Mira	Molly	Molly	Sara
	Zoey	Sara		Zoey		Zoey	Zoey	Zoey	

- Hiring priorities

1st	DM	Molly	Zoey	
2nd	ML	Gina	Laura	Kim
3rd	AI	Mira	Sara	

# Instant Run-Off Voting



- IRV is gaining popularity around the world (Australia, Ireland, Cambridge USA, NYS USA)
- IRV properties
  - proportional representation of solid coalition
  - promotes anti-plurality
  - reduces conflict within the electorate
  - reduces strategic voting
  - amenable to incomplete ranked order
  - representativeness in query results [Behar & Cohen, SIGMOD 2022]

# $k$ -Winners Selection



- Users (Voters) cast ballots, which are ranked orders of candidates
- Each candidate belongs to one out of  $k$  groups
- Select  $k$  winners, one winner per group, that represent the voters' preferences
- Motivation: fairness and priority
- Approach: find a “minimal manipulation” of the ballots that guarantees the selection from the required groups

# Constructive Margin of Victory (MOV)



- Number of ballot modifications required to guarantee winner from a given group

1 <sup>st</sup>	DM	Molly	Zoey	
-----------------	----	-------	------	--

						1	2	3	4	5	6	7	8	9	10
						Molly	Molly	Molly	Molly	Molly	Molly	Molly	Molly	Molly	Molly

Mira   Gina   Kim   Laura   Zoey   Sara

- **Theorem:** Computing the constructive margin of victory is **NP-Complete**, even for ballot size 2
- **Theorem:** Computing the constructive margin of victory can be formulated as an **integer linear program (IP)**

$$\begin{aligned}
 & \min \sum_{s \in S} a_s \quad \text{subject to} \\
 & m_s + a_s - d_s = y_s \quad \forall s \in S \quad (1) \\
 & m \geq y_s \geq 0 \quad \forall s \in S \quad (2) \\
 & m_s \geq d_s \geq 0 \quad \forall s \in S \quad (3) \\
 & m - m_s \geq a_s \geq 0 \quad \forall s \in S \quad (4) \\
 & \sum_{s \in S} a_s = \sum_{s \in S} d_s \quad (5) \\
 & u_{c_i, c_j} + u_{c_j, c_i} = 1 \quad \forall \{c_i, c_j\} \subseteq C \quad (6) \\
 & u_{c_i, c_j} + u_{c_j, c_r} + u_{c_r, c_i} \geq 1 \quad \forall \{c_i, c_j, c_r\} \subseteq C \quad (7) \\
 & v_{s, c_i, \tilde{c}} = u_{c_i, \tilde{c}} \cdot \prod_{x=1}^{i-1} u_{\tilde{c}, c_x} \quad \forall s \in S \forall \tilde{c} \in C \quad (8) \\
 & \sum_s (y_s \cdot v_{s, \hat{c}, \tilde{c}}) \geq u_{\hat{c}, \tilde{c}} \cdot \sum_s (y_s \cdot v_{s, \tilde{c}, \hat{c}}) \quad \forall \{\hat{c}, \tilde{c}\} \subseteq C \quad (9)
 \end{aligned}$$

# A Branch and Bound Algorithm

- Based on the framework given in [Magrino et al. EVT/WOTE 2011] and [Blom et al. INFORMS 2019] for **destructive margin of victory** computation
- **Enumerate** over all the **elimination orders** that end with a winner from the desired set to find the one with the least number of modifications

# A Branch and Bound Algorithm (cont.)



```
AlgExact( $B, C, W$ )
```

```
ub = MqIRVUB( $B, C, W$ )
```

```
initialize a priority queue PQ with  $(w, 0) \forall w \in W$ 
```

```
while PQ is not empty
```

```
    retrieve a minimum element  $(\pi, lb)$ 
```

```
    for  $c \in C - \pi$ 
```

```
         $\pi = c + \pi$  /* extend the elimination sequence  $\pi$  by  $c$ 
```

```
         $lb = \text{DistToLB}(B, C, \pi)$  /* lower bound on # of modifications
```

```
        if  $lb \leq ub$  insert  $(\pi, lb)$  to PQ
```

```
        if  $|\pi| = |C|$ 
```

```
             $ub = \min(ub, \text{DistTo}(B, C, \pi))$  /* compute the exact # of  
                                           /* modifications using IP
```

```
return ub
```

- A **tighter lower bound** and the **use of an upper bound** results in improved efficiency than previous work



# Computing DistTo



- $\text{DistTo}(B, C, \pi)$ : the minimum number of ballot “manipulations” required to achieve an elimination sequence
- **Theorem:** Computing  $\text{DistTo}$  in case of ballot modifications is NP-Complete, even for ballot size 3.
- **Theorem:**  $\text{DistTo}$  in case of ballot additions can be computed in polynomial time

Preference elicitation	Aggregation model	Output	Fairness	Approach
Score based	Average relevance, Least Misery	Top-k set	m-proportionality, m-envyfreeness, dissatisfaction score	Minimizing unfairness subject to quality constraints
Ranked order	Kemeny	Ranked k items	Top-k parity defined on a single binary or multi protected attribute	Find closest ranking that satisfies fairness
Ranked order	Kemeny, Spearman's footrule	Full rank	p-fairness defined on a single binary or multi protected attribute	Find closest ranking that satisfies fairness
Plurality	Plurality voting	Top-k set	Multiple protected attributes that may not be independent	Compute constructive MOV
Ranked order upto index l	Instant run off voting	Single winner	Fairness defined on a single protected attribute	Compute constructive MOV

# Part III – Future Research Directions (30 min)

## III-A : New Preference Aggregation Methods

- Producing structurally-involved outputs
- Dealing with uncertainties
- Going perpetual

## III-A : New Preference Aggregation Methods

- **Producing structurally-involved outputs**
- Dealing with uncertainties
- Going perpetual

## III-A : New Preference Aggregation Methods

- Beaten path
  - Single-winner > multiwinner > participatory budgeting
- Application-driven route (off the beaten path)
  - Resource allocation
  - Text aggregation

# III-A : New Preference Aggregation Methods

## Water distribution

### Fair Division with Storage

Eyal Briman<sup>1</sup>, Nimrod Talmon<sup>1</sup>, Stephane Airiau<sup>2</sup>, Umberto Grandi<sup>3</sup>, Jerome Lang<sup>2</sup>, Jerome Mengin<sup>3</sup> and Faria Nasiri Mofakham<sup>4</sup>

<sup>1</sup>Ben Gurion University of the Negev

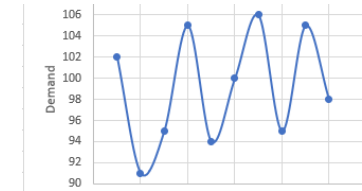
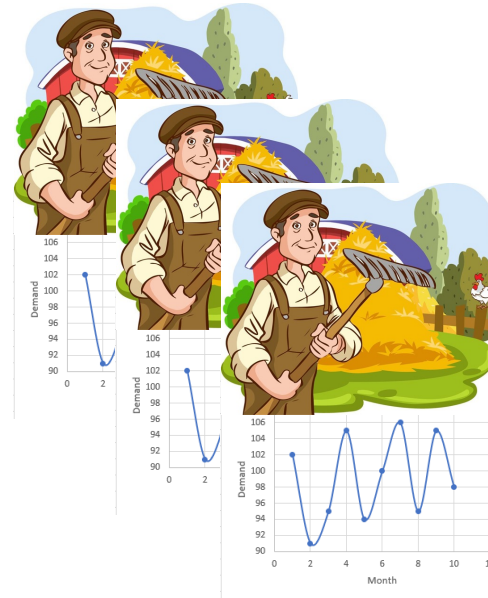
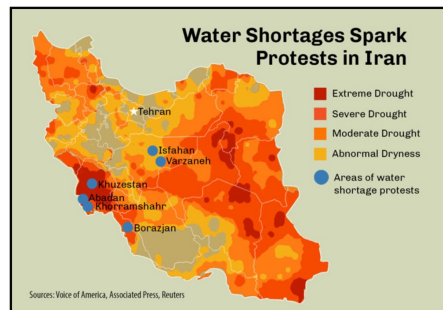
<sup>2</sup>Paris Dauphine University

<sup>3</sup>Toulouse University Capitole

<sup>4</sup>University of Isfahan

## III-A : New Preference Aggregation Methods

### Water distribution





# III-A : New Preference Aggregation Methods

## Text aggregation

Aggregation over Metric Spaces: Proposing and Voting in  
Elections, Budgeting, and Legislation

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### Abstract

We present a unifying framework encompassing a plethora of social choice settings. Viewing each social choice setting as voting in a suitable metric space, we offer a gen-

## AI-Generated Compromises for Coalition Formation

Anonymous

## Collaborative Document Writing: an Iterative Thresholds Approach

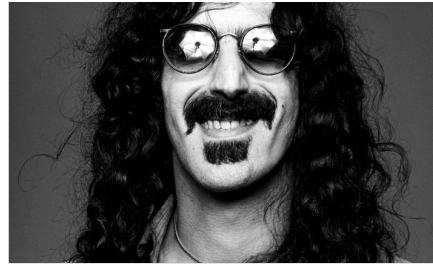
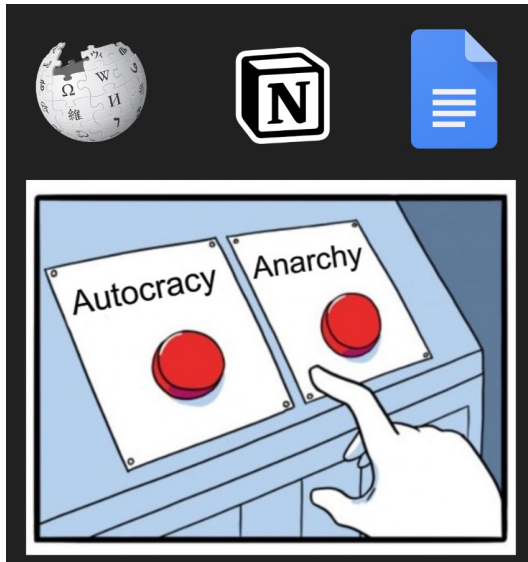
Avital Finanser

Nimrod Talmon

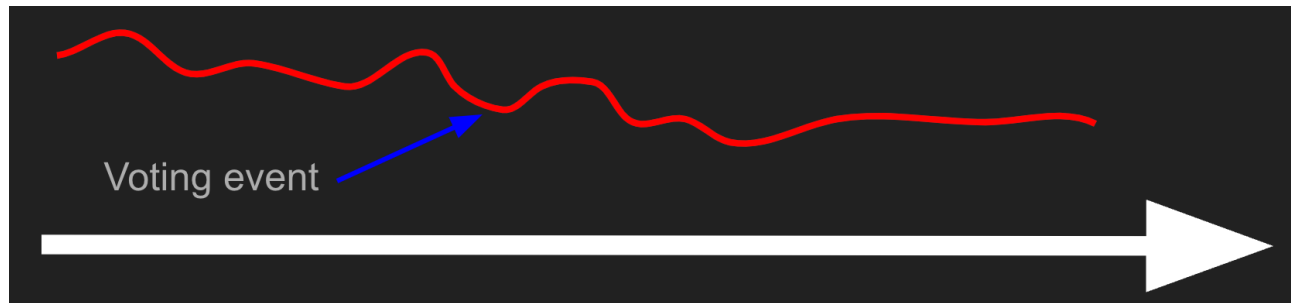
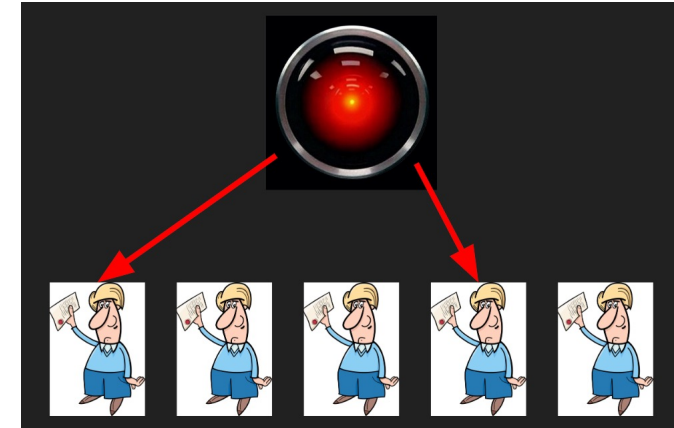
June 25, 2024

## III-A : New Preference Aggregation Methods

### Text aggregation



Put everything in a metric space!



## III-A : New Preference Aggregation Methods

- Aggregating more-involved preferences
- Outputting structurally-involved outputs
- **Dealing with uncertainties**
- Going perpetual

# III-A : New Preference Aggregation Methods

## • Dealing with uncertainties

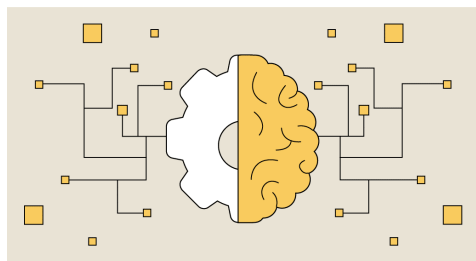
### A Recommendation System for Participatory Budgeting

#### Using Liquid Democracy for Attention-Aware Social Choice

Shiri Alouf-Heffetz

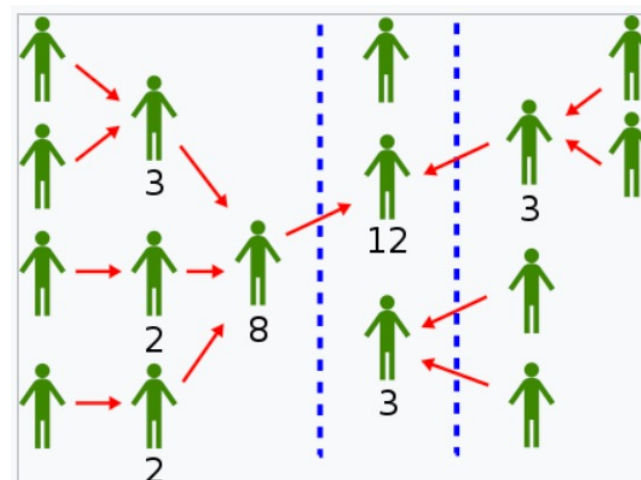
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3DOL  
Big Data Analytics Lab

<p><b>Culture &amp; Community Facilities</b></p> <p><input type="checkbox"/> A. Mural Project at Bennett Field \$22,000 Bennett Field Fieldhouse, Rindge Ave A middle school student in North Cambridge proposed installing a mural in his neighborhood that "shows the community of Cambridge". The mural will be installed on the Bennett Field Fieldhouse.</p> <p><input type="checkbox"/> B. Furniture for the O'Connell Library \$36,000 O'Connell Library 100 South Street The furniture at the O'Connell Library is quite worn down. This proposal would provide the library with new tables, chairs, computer workstations, and bookshelves for parents and children to read together.</p> <p><input type="checkbox"/> C. Bilingual Books for Children Learning English \$7,500 Cambridge This will fund the purchase of 300+ bilingual books for Cambridge children in the "Agenda for Children's Library" initiative project who are learning English, learning to read, &amp; have limited/no access to books in their home language.</p> <p><input type="checkbox"/> D. Little Free Libraries (Book Exchanges) \$13,000 Little Free Libraries Informal Book Exchanges are already popular in Cambridge on streets and at the O'Connell Library. This project would install 13 Little Free Libraries to support literacy, community engagement, and fun throughout the streets of our city.</p> <p><input type="checkbox"/> E. Computers for the Community Learning Center \$7,000 Community Learning Center, 3 River Street At the CLC, students can improve their English or pursue a high school equivalency diploma. The CLC has 18 laptops and 12 desktops for 65 adult learners. Project would fund 20 additional laptops, keyboards, mice and storage can for the students.</p>	<p><b>Streetscape</b></p> <p><input type="checkbox"/> F. Bike Repair Station \$12,000 Bicycle Repair Station Install 8 bike repair stations with tools and bike pumps around the City to cyclists to quickly, easily, and freely fix routine bike problems. Locations include 2 libraries, 2 shops, 3 parks (includes Inman Sq), and Fresh Pond Parkway.</p> <p><input type="checkbox"/> G. Renovation of Ben Shalom at Conant Field &amp; Bridge Ave. \$15,000 Bridge Avenue at Conant Field, North Cambridge This project entails a major redesign and renovation, with community participation, of the 400 bus shelter. New features will include angled panels with cut-out figures and a roof almost reflector of nearby recreation and natural habitat.</p> <p><input type="checkbox"/> H. Working-Business: Neighborhood &amp; Commercial Identity \$15,000 11 City Profile Area of Cambridge Along business in 11 change high-traffic, high-density business and neighborhood areas to identify commercial and/or neighborhood specific local areas in Cambridge. This would support commerce, identity, and neighborhood strategy.</p> <p><input type="checkbox"/> I. Traffic Calming \$200,000 Traffic Calming Calming will be determined through a community process. A Dutch Traffic Calming, called "Safety School" in the U.S., is a permanent park for children to learn transportation etiquette by role playing. Kids take turns biking, walking, and driving a miniature tricycle in a safe environment.</p> <p><input type="checkbox"/> J. Bus Shelter Monitors with Real Time Arrival \$10,000 Bus Shelter Install 2 real time bus arrival monitors with digital displays at the bus shelter at Cambridge Street &amp; Hampshire Street and Cambridge Street &amp; Inman Street.</p>
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## III-A : New Preference Aggregation Methods

- Aggregating more-involved preferences
- Outputting structurally-involved outputs
- Dealing with uncertainties
- **Going perpetual**

## III-A : New Preference Aggregation Methods

- Perpetual voting
  - **Making repeated decisions**
  - While being fair to external properties!

	Monday	Tuesday	Wednesday	Thursday	Friday
Student 1	C	C	C	C	A,C
Student 2	A	A	A	A	B
Student 3	A,B	A	A,C	A	A
Student 4	A	A	B	C	A
Student 5	B,C	B	B	B,C	A

### Justified Representation for Perpetual Voting

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## III-A : New Preference Aggregation Methods

- Perpetual voting
  - Making repeated decisions
  - **While being fair to external properties!**

## III-B : Perpetual Axiomatic Properties related to Individual Fairness



- **(Could be treated as candidate's long term fairness)** Simple proportionality – In a sequence of  $n$  rounds, if each of the  $n$  voters prefers only one candidate and no voter changes their preference across rounds, the number of times a candidate gets selected is equal to the proportion of votes the candidate has received.
- **(Could be treated as voter's long term fairness)** Bounded dry spell - Given a sequence of  $n$  rounds, a voter  $v$  has a dry spell of length  $l$  if  $v$ 's preferred candidate(s) get selected in at most every  $l$  rounds.



***Voters and candidates.  $m$  users (voters) provide **top-1** preference over  $n$  candidates***

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12	Count
C1	1	1	0	1	0	0	1	0	0	0	0	0	4
C2	0	0	1	0	1	0	0	0	1	0	0	0	3
C3	0	0	0	0	0	1	0	0	0	0	0	1	2
C4	0	0	0	0	0	0	0	0	0	1	1	0	2
C5	0	0	0	0	0	0	0	1	0	0	0	0	1
C6	0	0	0	0	0	0	0	0	0	0	0	0	0

**After 12 rounds, C1 wins 4 times, C2 wins 3 times, C3 wins 2 times, C4 wins 2 times, C5 wins 1 time, and C6 wins 0 time**

**Voters and candidates.**  $m$  users (voters) provide **top-1** preference over  $n$  candidates

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12	Count
C1	1	1	0	1	0	0	1	0	0	0	0	0	4
C2	0	0	1	0	1	0	0	0	1	0	0	0	3
C3	0	0	0	0	0	1	0	0	0	0	0	1	2
C4	0	0	0	0	0	0	0	0	0	1	1	0	2
C5	0	0	0	0	0	0	0	1	0	0	0	0	1
C6	0	0	0	0	0	0	0	0	0	0	0	0	0

If the sequence of winning candidates in 12 rounds are C1, C2, C3, C4, C5, C1, C2, C3, C4, C5, C1, C2, every voter has a bounded dry spell of 4!

## III-C : Technical Problems



- Is it possible to design a sequence of winners that satisfies
  - Perpetual axioms (e.g., simple proportionality/ bounded dry spell) **AND**
  - Group fairness (p-fairness or its relaxed version)?
- Depends on input - Does not seem to be always possible!
- How to minimally change input preferences such that a sequence of designed candidates simultaneously satisfies simple proportionality and p-fairness?
- How to design a sequence of candidates that satisfies **simple proportionality** and **satisfies p-fairness as closely** as possible?

## III-B : Alternative models for p-Fairness

- p-fairness may be too restrictive requirement
- Relaxed p-fairness 1: every prefix has “roughly” the proportionate number of occurrences from every protected attribute
  - The amount of deviation can be controlled
- Relaxed p-fairness 2: impose the proportionality constraints only at selected prefixes, e.g., every 10-percentile

## III-C : Technical Problems

- Does there exist any relationship between bounded dry spell and p-fairness?
  - When a voter selects only 1 preferred candidate
  - When a voter selects a subset of candidates as their preference
- can we approximate the margin of victory (either destructive or constructive) of IRV and STV in polynomial time?
- can we improve the computational efficiency of margin computation

## III-C : Technical Problems

- Handling more than one protected attribute in parallel. For example, guarantee fairness based on two protected attributes: gender and race.
- A simplistic approach is to assume that the attributes are independent and then consider the Cartesian product of the domains.
- Can this be done without assuming independence?

# Team and Collaborators



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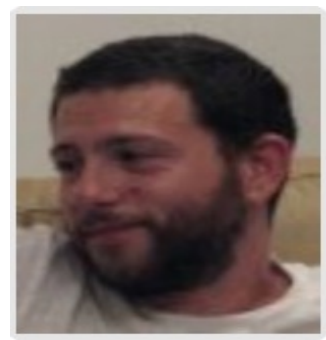
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Thank you – Questions?